

**REVIEW OF TRANSFORMATIONS
GEOMETRY**

Rigid motion – A transformation that preserves distance and angle measure (*the shapes are congruent, angles are congruent*).

Isometry – A transformation that preserves distance (*the shapes are congruent*).

Direct Isometry – A transformation that preserves orientation, the order of the lettering (ABCD) in the figure and the image are the same, either both clockwise or both counterclockwise (*the shapes are congruent*).

Opposite Isometry – A transformation that **DOES NOT** preserve orientation, the order of the lettering (ABCD) is *reversed*, either clockwise or counterclockwise becomes clockwise (*the shapes are congruent*).

Composition of transformations – is a combination of 2 or more transformations. In a composition, you perform each transformation on the image of the preceding transformation. *Example:* $r_{x\text{-axis}} \circ R_{0,180^\circ}$, the little circle tells us that this is a composition of transformations, we also execute the transformations from right to left ← (backwards).

If you would like a visual of this information or if you would like to quiz yourself, go to <http://www.mathsisfun.com/geometry/transformations.html>.

Line Reflection	Point Reflection	Translations (Shift)	Rotations (Turn)	Glide Reflection	Dilations (Multiply)
Rigid Motion	Rigid Motion	Rigid Motion	Rigid Motion	Rigid Motion	Not a rigid motion
Opposite isometry	Direct isometry	Direct isometry	Direct isometry	Opposite isometry	NOT an isometry
Reverse orientation	Same orientation	Same orientation	Same orientation	Reverse orientation	Same orientation
Properties preserved: 1. Distance 2. Angle measure 3. Parallelism 4. Collinearity 5. Midpoint	Properties preserved: 1. Distance 2. Angle measure 3. Parallelism 4. Collinearity 5. Midpoint	Properties preserved: 1. Distance 2. Angle measure 3. Parallelism 4. Collinearity 5. Midpoint	Properties preserved: 1. Distance 2. Angle measure 3. Parallelism 4. Collinearity 5. Midpoint	Properties preserved: 1. Distance 2. Angle measure 3. Parallelism 4. Collinearity 5. Midpoint	Properties preserved: 1. Angle measure 2. Parallelism 3. Collinearity 4. Midpoint Lengths NOT the same
Notation: $r_{x\text{-axis}}(x, y) = (x, -y)$ $r_{y\text{-axis}}(x, y) = (-x, y)$ $r_{y=x}(x, y) = (y, x)$ $r_{y=-x}(x, y) = (-y, -x)$	Notation: $r_{origin}(x, y) = (-x, -y)$	Notation: $T_{ab}(x, y) = (x + a, y + b)$	Notation: $R_{90^\circ}(x, y) = (-y, x)$ $R_{180^\circ}(x, y) = (-x, -y)$ $R_{270^\circ}(x, y) = (y, -x)$	Reflection and Translation *the translation HAS to be parallel to the line of reflection.	Notation: $D_k(x, y) = (kx, ky)$