

Topic 4A: Energy Work and Power

Skill 29: Work Energy Theorem

Work done equals energy change

$W = Fd$ where direction of force agrees with displacement

Identify Axis or scenario

- Work done vertically equals work done against gravity, i.e. gravitational potential energy

$$W_{\text{vertical}} = F_g d = F_g h = mgh = PE \quad (\text{for a ramp use only height})$$

$$W = PE \\ F_g d = mgh$$

- Work done horizontally to increase the speed of an object equals Kinetic Energy (assume frictionless)

$$W_{\text{horizontal}} = F_{\text{net}} d = (ma)d = m(ad) = \frac{1}{2}mv^2$$

$$\begin{aligned} v_f^2 &= v_i^2 + 2ad \\ v^2 &= 2ad \\ ad &= \frac{v^2}{2} \text{ or } \frac{1}{2}v^2 \end{aligned}$$

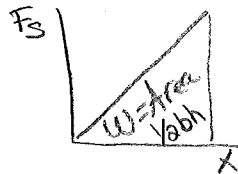
$$W = KE \\ F_x d = \frac{1}{2}mv^2$$

- Work done on a spring is equal to Elastic Potential Energy

$$W_{\text{spring}} = \overline{F}_s d = \overline{F}_s x = (\frac{1}{2}kx)x = \frac{1}{2}kx^2 \quad \overline{F}_s = \text{average spring force}$$

$$W = PE_s \\ \overline{F}_s d = \frac{1}{2}kx^2$$

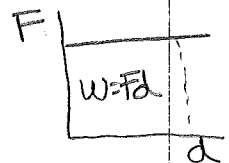
- Can also be found as area of F_s vs x graph



$$\text{area} = \frac{1}{2} F_s x \quad (\text{where } \overline{F}_s = kx)$$

$$\begin{aligned} \text{so } &= \frac{1}{2}(kx)(x) \\ &= \frac{1}{2}kx^2 \end{aligned}$$

For Non-springs
ON A Graph
of F vs d (h)
Work is area



- Work done by friction (Q) - aka. Internal Energy

$$W_{\text{friction}} = F_f d = Q$$

$$E_T = KE + PE + Q$$

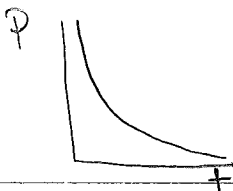
$$\text{so } Q = E_T - (KE + PE)$$

Skill 30: Power

Power is the RATE at which energy is used or work is done

$$P = \frac{W}{t} = \frac{Fd}{t} = Fv$$

Scalar quantity measured
in Watts = $\frac{\text{Joule}}{\text{second}} = \frac{\text{Nm}}{\text{s}}$



Power and time
are inversely related
for a fixed (constant)
work value



Power is directly
related to speed at
which a fixed work
is done